

Ques 2: $\int \frac{\cos \theta}{(1+\sin \theta)(2+\sin \theta)} d\theta$

let $\sin \theta = t$

$\cos \theta d\theta = dt$

$\int \frac{dt}{(1+t)(2+t)}$

By using fractional method.

$$\frac{1}{(1+t)(2+t)} = \frac{A}{(1+t)} + \frac{B}{(2+t)}$$

$$1 = (2+t)A + B(1+t)$$

$$1+t=0$$

put $t = -1$

$A = 1$

$t = -2 \quad B = 2$

$$\int \frac{1}{(1+t)(2+t)} dt = \int \frac{1}{(1+t)} + \left(\frac{2}{(2+t)} \right) dt$$

$$= \log(1+t) + 2 \log(2+t) + C$$

$$= \log(1+\sin \theta) + 2 \log(2+\sin \theta) + C$$