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$$g(x) = ax^2 + bx + c \quad [-h, h]$$

$$\int_{-h}^h g(x) dx = \int_{-h}^h ax^2 + bx + c$$

$$\Rightarrow \left[ \frac{ax^3}{3} + \frac{bx^2}{2} + cx - \left( \frac{ah^3}{3} + \frac{bh^2}{2} - ch \right) \right]$$

$$\Rightarrow \frac{ah^3}{3} + \frac{bh^2}{2} + ch + \left[ -\frac{ah^3}{3} + \frac{bh^2}{2} - ch \right]$$

$$\Rightarrow \frac{ah^3}{3} + \frac{bh^2}{2} + ch + \frac{ah^3}{3} - \frac{bh^2}{2} + ch$$

$$\Rightarrow \frac{2}{3} ah^3 + 2ch$$

$$\Rightarrow \frac{h}{3} [2ah^2 + 6c] - \textcircled{A}$$

$$g(x) = ax^2 + bx + c$$

$$f(-h) = g(-h) = ah^2 - bh + c \quad \textcircled{1}$$

$$f(0) = g(0) = c \quad \textcircled{2}$$

$$f(h) = g(h) = ah^2 + bh + c \quad \textcircled{3}$$

adding ① and ③

$$f(-h) + f(h) = 2ah^2 + 2c$$

$$\Rightarrow y_0 + y_2 = 2ah^2 + 2y_1$$

$$\Rightarrow \boxed{2ah^2 = y_0 - 2y_1 + y_2}$$

Substitute the value of solution ④ we get

$$\Rightarrow \frac{h}{3} [y_0 - 2y_1 + y_2 + 5y_1]$$

$$\frac{h}{3} [y_0 + 4y_1 + y_2] \approx \int_{-h}^h f(x) dx$$

$$\frac{h}{3} [y_2 + 4y_3 + y_4] \dots$$

while points are  $(x_2, y_2)$ ,  $(x_3, y_3)$  and  $(x_4, y_4)$

$$\frac{h}{3} [y_{n-3} + 4y_{n-1} + y_n]$$

$$\int_a^b f(x) dx = \frac{h}{3} [(y_0 + y_n) + 4(y_1 + y_2 + y_3 + \dots + y_{n-1}) + 2(y_2 + y_4 + y_6 + \dots + y_{n-2})]$$

(ii)  $\int \frac{x-1}{x+1} dx$ ?

Ans  $\int \frac{x-1}{x+1} dx = x - 2 \ln |x+1| + C$

$$\int \frac{x+1}{x+1} dx \rightarrow \int \frac{x+1-2}{x+1} dx =$$

$$\int \left( 1 - \frac{2}{x+1} \right) dx$$

$$\int \frac{x-1}{x+1} dx = \int (x-2) \frac{dx}{x+1}$$

$$\frac{x-1}{x+1} dx = x-2 \ln|x+1| + C$$

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 \quad \text{--- ~~यह एक वृत्त है~~ ---}$$