

- ① What do you understand by resolving power. Deduce the expression for resolving power of grating.

Ans Resolving power of grating

It is defined as the ratio of wavelength ( $\lambda$ ) of any spectral line to the smallest difference of two wavelengths ( $d\lambda$ ), for which the spectral lines can be resolved at the wavelength.

$$\text{Resolving power of grating} = \frac{\lambda}{d\lambda}$$

Expression - Let a light consisting of two wavelengths ( $\lambda_1$  and  $\lambda_2$ ) of any spectral line is incident normally on a grating element ( $e+d$ ) and the spectral lines corresponding to  $\lambda_1$  and  $\lambda_2$  are focused on screen  $P_1$  and  $P_2$ .

- ② These spectral lines just resolve if they satisfy the Rayleigh's criterion. The direction of  $n^{\text{th}}$  principal maxima for wavelength  $\lambda_1$  is given by

$$(e+d) \sin \theta = n \lambda_1$$

$$N(e+d) \sin \theta = N n \lambda_1$$

- ③ And 1<sup>st</sup> minima in direction ( $\theta = d\theta$ ) is

$$N(e+d) \sin (\theta + d\theta) = n \lambda_1$$

except  $(m=0, N, 2N, \dots$  or  $1, 2, 3, \dots, N-1)$

When  $m = n(N+1)$ , e.g.

$$N(e+d) \sin(\theta + d\theta) = (nN+1) \lambda_1$$

The principal maxima due to wavelength  $\lambda_2$  in direction  $(\theta + d\theta)$  is  $(e+d) \sin(\theta + d\theta) = n\lambda_2$

$$N(e+d) \sin(\theta + d\theta) = Nn\lambda_2$$

⑥ Comparing eq, we get,

$$(nN+1) \lambda_1 = Nn\lambda_2$$

⑦ if  $\lambda_1 = \lambda$ ,  $\lambda_2 = \lambda + d\lambda$   $d\lambda = \lambda_2 - \lambda_1$  e.g.

$$N(N+1) \lambda = Nn(\lambda + d\lambda)$$

$$\text{or } \lambda = Nnd\lambda \quad \text{or} \quad \frac{\lambda}{d\lambda} = nN$$

$$\text{But } (e+d) \sin\theta = n\lambda$$

$$\text{or } n = \frac{(e+d) \sin\theta}{\lambda}$$

$$\boxed{\frac{\lambda}{d\lambda} = \frac{N(e+d) \sin\theta}{\lambda}}$$