

Resolving Power

The ability of an optical instrument to produce the separate images of two objects placed very close to each other is known as resolving power.

Expression:

Let a light consisting of two wave lengths λ_1 and λ_2 is incident normally on a grating element $(e+d)$ and the spectral lines corresponding to λ_1 and λ_2 are formed on screen P_1 and P_2 .

These spectral lines, just resolve if they satisfy the Rayleigh's criterion, the direction of n^{th} principal maxima for wave-length (λ_1) is given by

$$(e+d) \sin \theta = n \lambda_1$$

$$N (e+d) \sin \theta = N n \lambda_1$$

and 1st minima in direction $(\theta + d\theta)$ is

$$N (e+d) \sin \theta = N n \lambda_1.$$

except ($m = 0, N, 2N \dots$)

when $m = (nN + 1)$, eq (4.26.2) becomes

$$N(e + d) \sin(\theta + d\theta) = (nN + 1)\lambda_1$$

The Principal maxima due to wave-length λ_2 in direction $(\theta + d\theta)$ is

$$(e + d) \sin(\theta + d\theta) = n\lambda_2$$

$$N(e + d) \sin(\theta + d\theta) = Nn\lambda_2$$

Comparing eq we get

$$(nN + 1)\lambda_1 = Nn\lambda_2$$

$$\text{if } \lambda_1 = \lambda, \lambda_2 = \lambda + d\lambda$$

$$d\lambda = \lambda_2 - \lambda_1, \text{ eq becomes}$$

$$(nN + 1)\lambda = Nn(\lambda + d\lambda)$$

$$\text{or } \lambda = Nn d\lambda \quad \text{or } \frac{\lambda}{d\lambda} = nN$$

$$\text{But } (e + d) \sin \theta = n\lambda \quad \text{or } n = \frac{(e + d) \sin \theta}{\lambda}$$

$$\frac{\lambda}{d\lambda} = \frac{N(e + d) \sin \theta}{\lambda}$$