

### Question - 4

(ii) what are the properties of double integration?

Ans  $\Rightarrow$  Function of two variables:  $f(x, y)$   
 $f(u, v), g(x, y)$

Independent variables:  $x, y, u, v$

Small changes:  $\Delta x, \Delta y$

Regions of integration:  $R, S$

Real numbers:  $a, b, c, d, \alpha, \beta$

polar coordinates :  $r, \theta$   
Area of a region :  $A$   
Surface area :  $S$   
Volume of a solid :  $V$   
Mass of a lamina :  $m$   
Density of a lamina :  $\rho(x, y)$   
First moments :  $M_x, M_y$   
Moments of inertia :  $I_x, I_y, I_0$   
Charge of a plate :  $Q$   
Charge density :  $\sigma(x, y)$   
Coordinates of the center of mass :  $\bar{x}, \bar{y}$   
Average of a function :  $\bar{f}$

## Section - 4

Question

Q.9: (i)

$$\text{Evaluate } \int_0^1 \int_x^{0.5} (x^2 + y^2) \, dx \, dy$$

$$= \int_0^1 \left[ \frac{x^2 y + y^3}{3} \right]_x^{0.5} \, dy$$

$$= \int_0^1 \left( \frac{x^2 y + y^3}{3} \right) \, dy$$

$$= \frac{1}{3} \left[ \frac{x^3 y + \frac{1}{5} y^5}{5} \right]_x^{0.5}$$

$$= \frac{1}{3} ab^3 + \frac{1}{3} a^3 b$$

$$= \frac{1}{3} ab(a^2 + b^2) \quad \text{A}$$