

Q8

Calculate quantiles of the following distribution: -

Age Group	f	C.f
25-30	10	10
30-35	12	22
35-40	25	47
40-45	40	87
45-50	10	97
50-55	3	100
	N=100	

Solⁿ → (1) Q_1 Class = $\frac{N}{4} = \frac{100}{4}$ $Q_1 = 25$

$$Q_1 = l_1 + \left(\frac{N/4 - C.f}{f_{Q_1}} \right) \times i$$

$$= 30 + \left(\frac{100 - 10}{4} \right) \times 5$$

$$= 30 + \left(\frac{90}{4} \right) \times 5$$

$$Q_1 = 30 + 112.5$$
 $Q_1 = 142.5$

(2) $Q_2 = \frac{N}{2} = \frac{100}{2} = \mathbf{Q_2 = 50}$

$l_1 = 35$, $\Sigma f_1 = 22$, $f_{Q_2} = 25$, $i = 5$

$$Q_2 = l_1 + \left(\frac{N/2 - \Sigma f_1}{f_{Q_2}} \right) \times i$$

$$= 35 + \left(\frac{\cancel{100} 50 - 22}{25} \right) \times 5$$

$$= 35 + \frac{28}{25} \times 5$$

$$= 35 + 1.12 \times 5$$

$$= 35 + 5.6$$

$$\boxed{Q_2 = 40.6}$$

$$\textcircled{3} \quad Q_3 \text{ class} = \frac{3}{4} (N)$$

$$= \frac{3}{4} (1000)$$

$$= \frac{3000}{4} = 750$$

$$l_1 = 40, \quad \sum f_1 = 47, \quad fd_3 = 40, \quad c' = 5$$

$$Q_3 = l_1 + \left(\frac{\frac{3N}{4} \cdot \sum f_1}{fd_3} \right) \times c'$$

$$= 40 + \frac{750 - 40}{40} \times 5$$

$$= 40 + \frac{710}{40} \times 5$$

$$= 40 + \frac{355}{40} \times 5$$

$$= 40 + 3.87$$

$$\boxed{Q_3 = 43.87}$$