

Section - 5

Q1

Ans. Bending Equation :-

Bending theory is also known as flexure theory & is defined as the axial deformation of the beam due to external load that is applied perpendicular to a longitudinal axis which finds application in applied mechanics.

- For a material, flexural strength is defined as the stress that is obtained from the yield just before the flexure test.
- It represents the highest stress that is experienced within the material at the moment of its yield.
- " σ " is used as the symbolic representation of flexural strength.

* Bending Equation Derivation :-

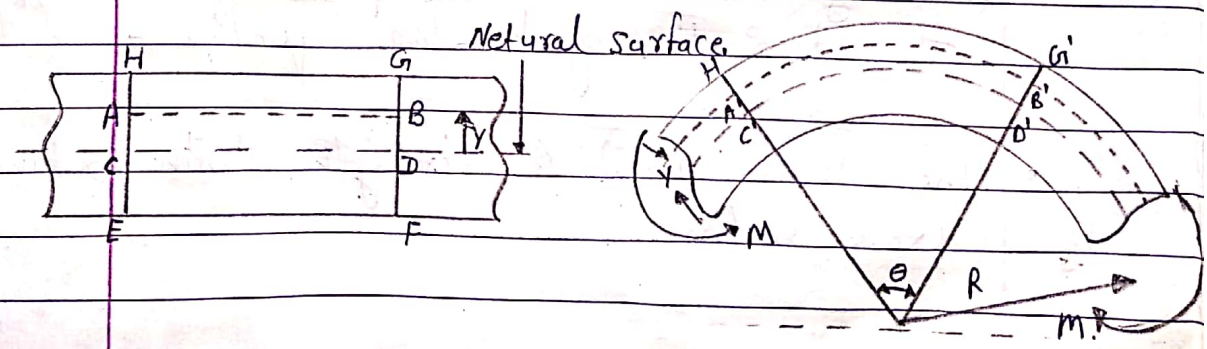
Following are the assumptions made before the derivation of bending equation :-

- The beam used is straight with constant cross-section.

- The beam used is of homogeneous material with a symmetrical longitudinal plane.
- The plane of symmetry has all the resultant of applied loads.
- The primary cause of failure is buckling.
- E remain same for tension and compression.
- Cross section remains the same before and after bending.

⇒ Consider an unstressed beam, which is subjected to a const. bending moment such that the beam bends up to radius R .

- The top fibres are subjected to tension whereas the bottom fibres are subjected to compression.
- The locus of points with 'zero' stress is known as "neutral axis".



• With the help of the above fig., the following are the steps involved in the derivation of the bending equation:

• Strain in fibre AB is the ratio of change in length to original length.

• Strain in fibre, AB = $\frac{A'B' - AB}{AB}$

∴ Strain = $\frac{A'B' - C'D'}{C'D'}$ (as AB = CD and CD = C'D')

• CD & C'D' are on the neutral axis and stress is assumed to be zero, therefore strain is also zero on the neutral axis.

$$= \frac{(R+y)\theta - R\theta}{R\theta}$$

$$= \frac{R\theta + y\theta - R\theta}{R\theta}$$

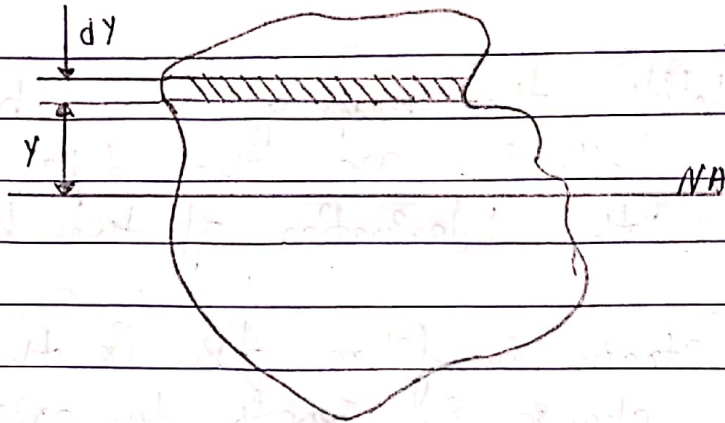
$$= \frac{y}{R}$$

$$\boxed{\frac{\sigma}{E} = \frac{y}{R}}$$

where :-

(E → Young's Modulus of Elasticity)

$$\boxed{\sigma = \frac{E y}{R}}$$



$$\sigma = \frac{E}{R} y \quad \text{--- (1)}$$

$$F = \sigma dA = \frac{E}{R} y dA \quad (\text{force acting on the strip with area } dA)$$

$$Fy = \frac{E}{R} y^2 dA \quad (\text{momentum about neutral axis})$$

$$M = \sum \frac{E}{R} y^2 \quad (\text{total momentum for entire cross-section area})$$

$$M = \frac{E}{R} \sum y^2 dA$$

" $\sum y^2 dA$ " is known as second moment of area and is represented as I

$$M = \frac{E}{R} I \quad \text{--- (2)}$$

from eqn (1) & eqn (2), we get

$$\frac{\sigma}{y} = \frac{M}{I} = \frac{E}{R}$$

Ans

Therefore, the above is the bending theory equation.