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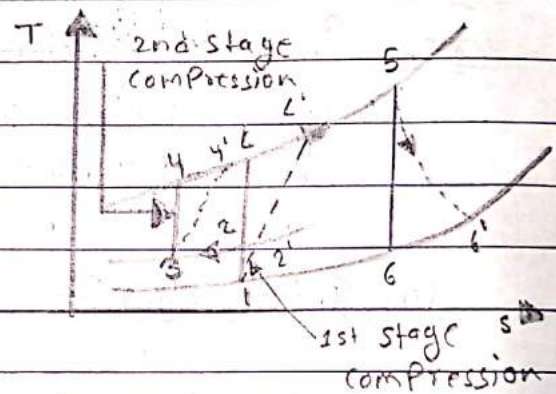
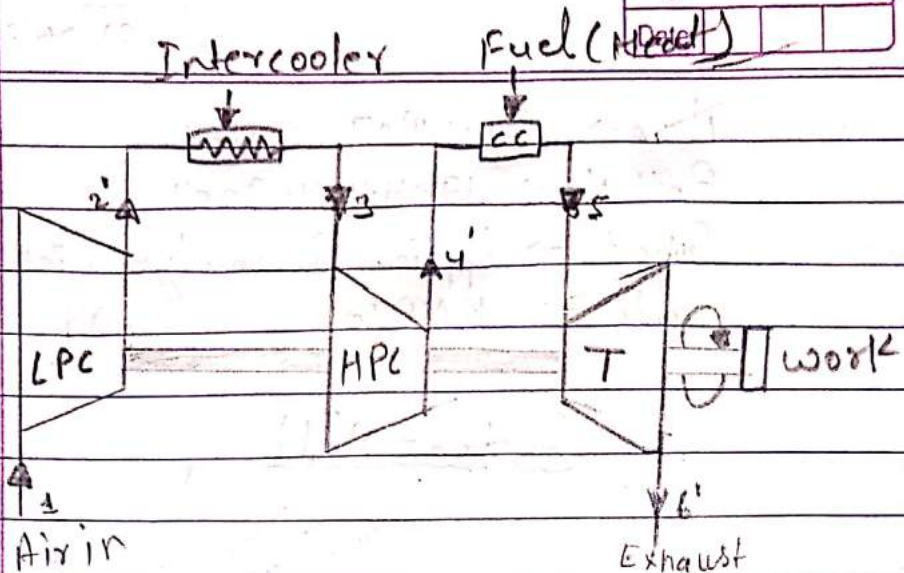
Section - (1)

Q1

Ans. Thermal efficiency or specific output of an open cycle gas turbine can be improved by following three methods:-

(a) Intercooling:-

- This is required to reduce the compressor work and to increase the work ratio.
- The compression of air is to be done in two compressors.
- Firstly in low pressure compressor then in high pressure compressor, compression process is to be done as shown in fig.
- Fig. shows ideal and actual processes which occur in an open cycle gas turbine. The dotted lines show the actual curve & thicker one shows the ideal curve.



• From T-s diagram,

(i) The process with intercooling is 1-2-3-4-5-6 (Ideal process) or 1-2'-3-4'-5-6' (Actual Process)

(ii) The work required to run the compressor with intercooling is,

For ideal conditions, $W_{c1} = C_p (T_2 - T_1) + C_p (T_4 - T_3)$
 For actual conditions, $W_{c1} = C_p (T_2' - T_1) + C_p (T_4' - T_3)$

(iii) The process 1-2-3-6 is ideal process without intercooling, whereas 1-2'-3-6' is actual process without intercooling.

(iv) The work required to run the compressor w/o intercooling is,

For ideal condition,

$$\begin{aligned}
 W_c &= C_p (T_L - T_1) \\
 &= C_p (T_L - T_2 + T_2 - T_1) \\
 &= C_p (T_L - T_2) + C_p (T_2 - T_1)
 \end{aligned}$$

For actual condition,

$$\begin{aligned}
 W_c &= C_p (T_{L'} - T_1) \\
 &= C_p (T_{L'} - T_{2'} + T_{2'} - T_1) \\
 &= C_p (T_{L'} - T_{2'}) + C_p (T_{2'} - T_1)
 \end{aligned}$$

- As it is clear from the T-s curve that

$$T_{L'} - T_2 > T_{4'} - T_3 \quad (\text{For actual process})$$

$$T_L - T_2 > T_4 - T_3 \quad (\text{For ideal process})$$

- But the heat supplied inc^(es) & this increase in heat supply leads to decrease in thermal efficiency.

(B) Reheating :-

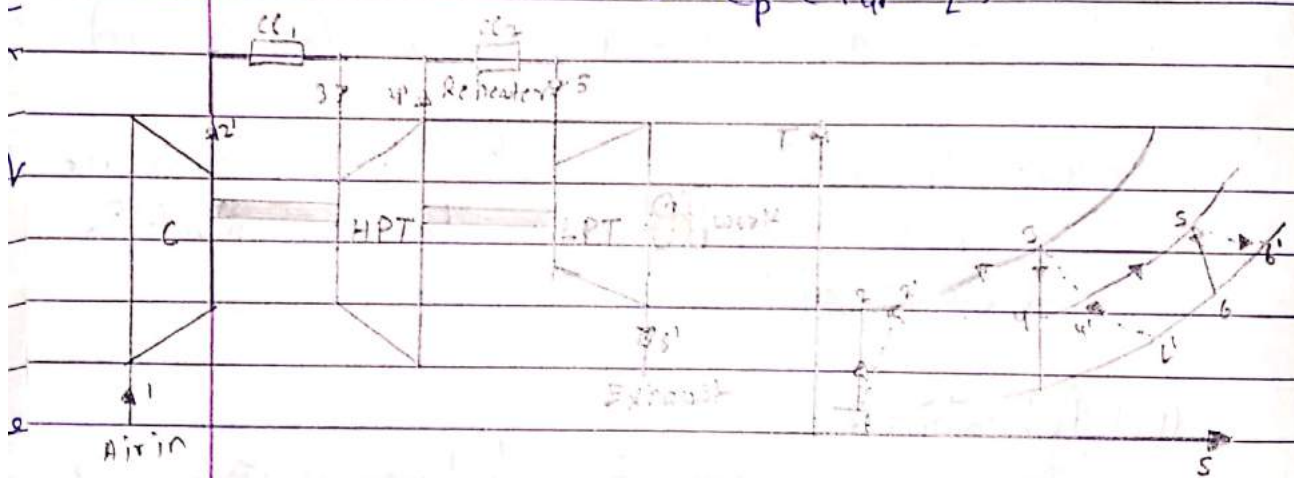
- This process uses two turbines a high press. turbine & a low press. turbine.
- There is a reheater present in b/w these two turbine.
- Here high press. turbine is used to drive the compressor & the low press. turbine provide useful work i.e. output.

- Actual process is shown by 1-2'-3-4-5-6' (with reheating) & ideal process is shown by 1-2-3-4-5-6 (with reheating).

- Actual process without reheating is shown by 1-2'-3-4' & the ideal process without reheating is shown by 1-2-3-4-1

The work output with reheating = $C_p (T_5 - T_6)$

The work output without reheating = $C_p (T_{4'} - T_{1'})$



- Hence the work output inc. (res) with reheating.
- This will also inc. (res) the work input & it may be result into reduction in thermal efficiency.

(c) Regeneration:-

- Regenerator is a heat exchanger which is used to preheat the air leaving compressor before entering the combustion chamber, thereby reducing the amount of fuel to be burnt inside combustion chamber (combustor).

- Under ideal conditions, no frictional press. drop occurs in either fluid stream while turbine exhaust gas gets cooled from 4 to $4'$ while compressed air is heated from 2 to $2'$.

- Regenerator effectiveness, $\epsilon = \frac{h_{2'} - h_2}{h_4 - h_2}$

- Thermodynamically the amount of heat added,

$$(Q_{add})_{regen} = m(h_3 - h_{2'})$$

whereas without regenerator the heat added,

$$Q_{add} = m(h_3 - h_2)$$

- Here it is obvious that, $(Q_{add})_{regen} < Q_{add}$ this shows an obvious improved in cycle thermal efficiency.

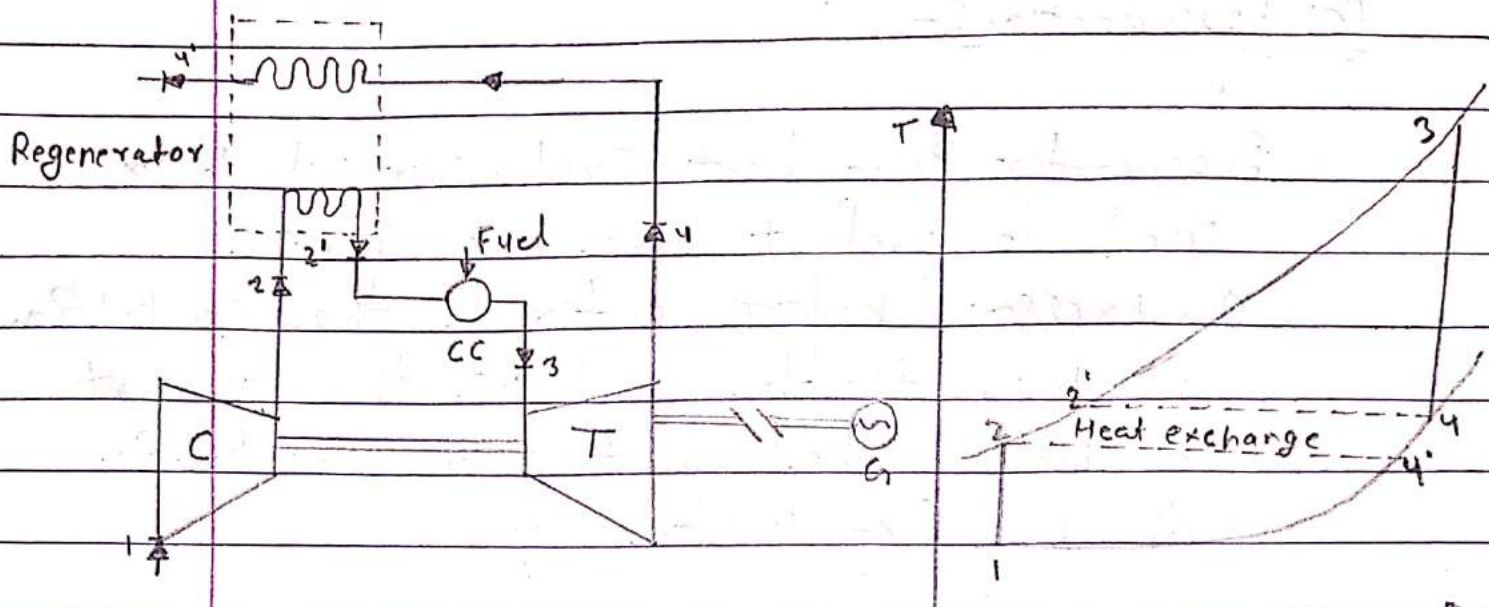
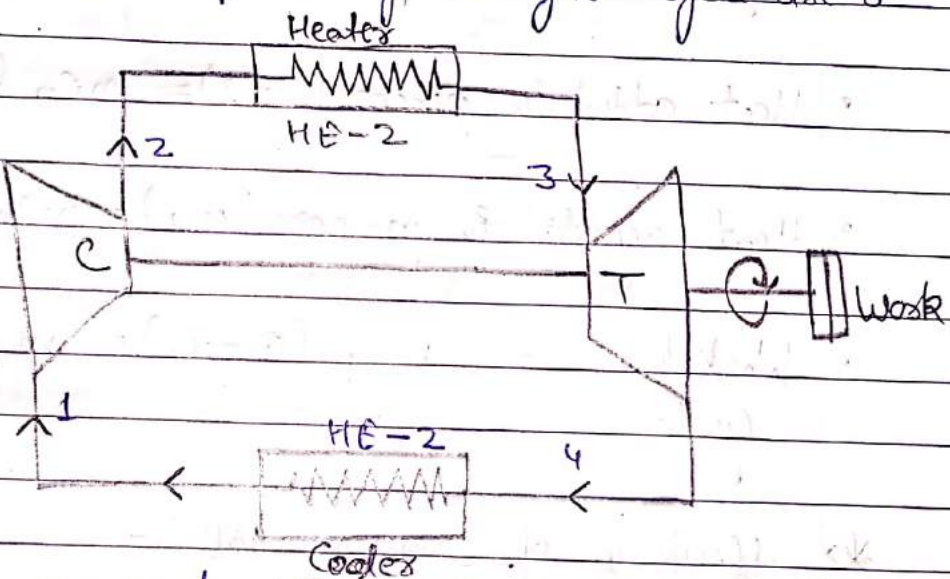


fig :- Regeneration

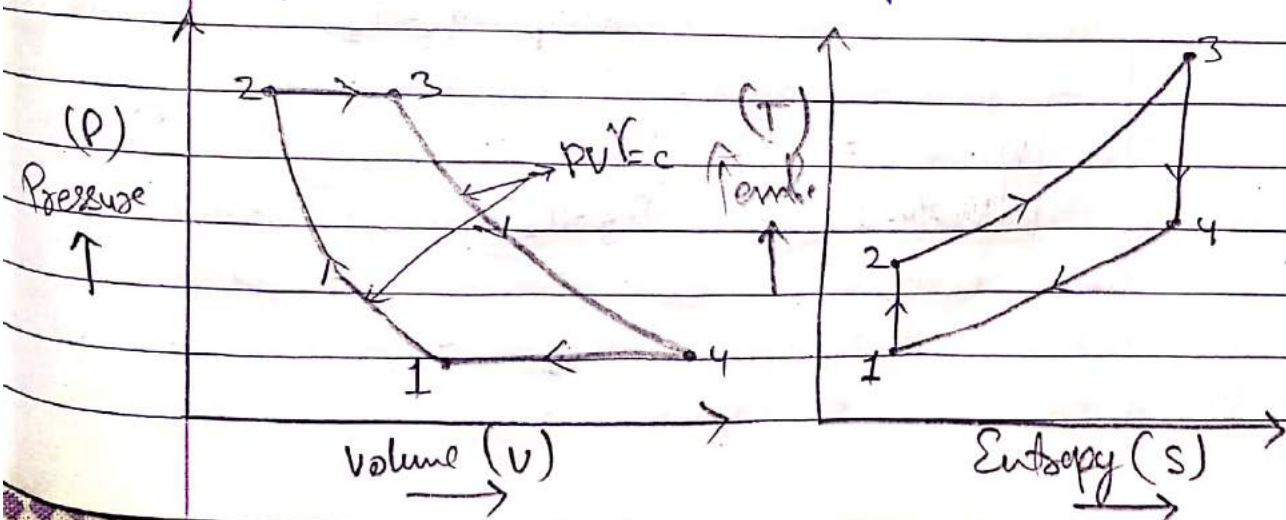
(2) Constant volume Combustion gas turbine.

Brayton Cycle :-

- It is a theoretical cycle for gas turbines and also known as constant pressure cycle for a perfect gas.
- The basic component of a Brayton cycle are :-



- There occur two isentropic processes & two constant pressure processes.
- Compression & expansion of working fluid is done by isentropic process while addition & rejection of heat is done at constant pressure.



*→ Brayton cycle shows following processes:-

(1-2) → Adiabatic Compression.

(2-3) → Constant pressure heat addition.

(3-4) → Adiabatic Expansion.

(4-1) → Constant pressure heat rejection.

- $$\frac{\text{Workdone}}{\text{Cycle}} = \frac{\text{Heat added}}{\text{Cycle}} - \frac{\text{Heat rejected}}{\text{Cycle}}$$

- Heat added in process (2-3) = $m c_p (T_3 - T_2)$

- Heat rejected in process (4-1) = $m c_p (T_4 - T_1)$

- $$\frac{\text{Workdone}}{\text{Cycle}} = m c_p (T_3 - T_2) - m c_p (T_4 - T_1)$$

*→ Efficiency of Brayton cycle:-

- Efficiency, $\eta_{\text{air-std.}}$ = $\frac{\text{Workdone / cycle}}{\text{Heat addition / cycle}}$

$$= \frac{m c_p (T_3 - T_2) - m c_p (T_4 - T_1)}{m c_p (T_3 - T_2)}$$

$$\eta_{\text{air-std.}} = 1 - \frac{T_4 - T_1}{T_3 - T_2} \quad \text{--- (1)}$$

- From process (1-2) -

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}}$$

$$\left(\because \frac{P_2}{P_1} = \sigma_p = \text{Press. ratio}\right)$$

$$T_2 = T_1 (\sigma_p)^{\frac{\gamma-1}{\gamma}}$$

- Similarly, from process (3-4)

$$\frac{T_3}{T_4} = \left(\frac{P_3}{P_4}\right)^{\frac{\gamma-1}{\gamma}} = (\sigma_p)^{\frac{\gamma-1}{\gamma}}$$

$$T_3 = T_4 (\sigma_p)^{\frac{\gamma-1}{\gamma}}$$

Now

- Putting the value of T_2 & T_3 in eqn (1), we get

$$\eta_{\text{air std.}} = 1 - \frac{T_4 - T_1}{T_4 (\sigma_p)^{\frac{\gamma-1}{\gamma}} - T_1 (\sigma_p)^{\frac{\gamma-1}{\gamma}}}$$

$$= 1 - \frac{(T_4 - T_1)}{(\sigma_p)^{\frac{\gamma-1}{\gamma}} (T_4 - T_1)}$$

$$\eta_{\text{air-standard}} = 1 - \frac{1}{(\sigma_p)^{\frac{\gamma-1}{\gamma}}}$$