

Q.2

Ans:

Suppose the coin is unbiased.  
then the probability of getting head in a  
toss =  $1/2$

$$\text{Expected no. of success} = 1/2 \times 400 = 200$$

$$\text{the observed value of success} = 216$$

$$\text{thus the excess of observed value over expected value} = 216 - 200 = 16$$

$$\text{SD of simple Sampling} = \sqrt{npq}$$

$$= \sqrt{(400 \times \frac{1}{2} \times \frac{1}{2})}$$

$$= 10$$

Hence

$$Z = \frac{x - np}{\sqrt{npq}} = \frac{16}{10} = 1.6$$

As  $Z < 1.96$ , the hypothesis is accepted at 5% level of significance i.e., we conclude that the coin is unbiased at 5% level of significance.

Null Hypothesis,  $H_0$ : Male and female are equally probable.

No. of boys	4	3	2	1	0
No. of girls	0	1	2	3	4
No. of families	10	55	105	58	12

Alternate hypothesis  $H_1$  :- Male and female birth are not equally probable. Calculation of expected frequencies  $(q+p)^n$ .

$$\text{Probability of female birth} = p = \frac{1}{2}$$

$$\text{Probability of Male birth} = q = \frac{1}{2}$$

$$(q+p)^n = q^n + {}^n C_1 pq^{n-1} + {}^n C_2 p^2 q^{n-2} + {}^n C_3 p^3 q^{n-3} \dots p^n \\ = \left(\frac{1}{2}\right)^4 + 4\left(\frac{1}{2}\right)^1 \left(\frac{1}{2}\right)^3 + 6\left(\frac{1}{2}\right)^2 \left(\frac{1}{2}\right)^2 + 4\left(\frac{1}{2}\right)^3 \left(\frac{1}{2}\right)^1 + \left(\frac{1}{2}\right)^4$$

$$\text{No. of girls} = 240 \left[ \frac{1}{16} + \frac{4}{16} + \frac{6}{16} + \frac{4}{16} + \frac{1}{16} \right]$$

$$= \frac{15}{240} \times \frac{1}{16} + \frac{15}{240} \times \frac{4}{16} + \frac{15}{240} \times \frac{6}{16} + \frac{15}{240} \times \frac{4}{16} + \frac{15}{240} \times \frac{1}{16} \\ = 15 + 60 + 90 + 60 + 15$$

These are the expected frequencies of female births.

O	E	O - E	$(O-E)^2$	$\frac{(O-E)^2}{E}$
10	15	-5	25	1.67
55	60	-5	25	0.41
105	90	15	225	2.5
58	60	-2	4	0.067
12	15	-3	9	0.6
		Total	5.247	

Given,  $\chi^2_{0.05} = 9.49$  and 11.1 for d.f. and 5d.f

since the calculated value of  $\chi^2(5.247) < \chi^2$  value at 4d.f and 5d.f.

Hence, the male and female birth is equally probable.