

Section 6

Question 2

Answer 2.

1. Let us assume L is regular, let p be a constant provided by the pumping lemma.
2. Let w be the string 0^3 . This string S is in L and its length is at least p . So w can be written as xyz with $|xy| \leq p$ and $x \neq \epsilon$.
3. Pumping lemma states that if $xyz \in L$ then xy^kz also is in L contains at least one 0 in y since y is not ϵ .
4. Let us assume for $k = 2$, the resulting string is xy^2z .
5. So it suffices to show that $p^3 < p^3 + p < (p+1)^3$. The first inequality holds since $p > 0$.
6. The claim is established, so xy^2z is not in L .
7. This contradicts the pumping lemma, so our original assumption, that L was regular is not correct.

The CFG can be given by production rule

$$(P) : \\ S \rightarrow OS/IS \\ S \rightarrow \epsilon$$

The rules add by the combination of 0's & is with the start with start symbol.