

Q2. A coin was tossed 400 times & the head turned up 216 times. Test the hypothesis that the coin is unbiased of 5% level of significance.

Sol

Suppose the coin is unbiased.  
Then the probability of getting the head in a toss =  $\frac{1}{2}$

$\therefore$  expected number of successes =  $\frac{1}{2} \times 400$   
The observed value of successes = 216

Thus the excess of observed value over expected value =  $216 - 200 = 16$

Also SD of simple sampling =  $\sqrt{npq}$   
 $= \sqrt{400 \times \frac{1}{2} \times \frac{1}{2}} = 10$

$$Z = \frac{\bar{x} - np}{\sqrt{npq}} = \frac{16}{10} = 1.6$$

As  $z < 1.96$ , the hypothesis is accepted at 5% level of significance, i.e., we conclude that the coin is unbiased at 5% level of significance.

11) A survey of 240 families with 4 children shows the following distribution:

no. of boys	4	3	2	1	0
no. of families	10	55	105	58	12

Test the hypothesis that male & female births are equal probable.

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Null hypothesis,  $H_0$ : Male & female are equally probable.

no. of boys	4	3	2	1	0
no. of girls	0	1	2	3	4
no. of families	10	55	105	58	12

$400 = 200$

Alternate hypothesis  $H_1$ : Male & female birth are not equally probable, calculation of expected frequencies  $(p+q)^n$

$$\text{probability of female birth} = p = \frac{1}{2}$$

$$\text{probability of male birth} = q = \frac{1}{2}$$

$$\begin{aligned} (p+q)^n &= q^n + {}^nC_1 p q^{n-1} + {}^nC_2 p^2 q^{n-2} + {}^nC_3 p^3 q^{n-3} + \dots \\ &= \left(\frac{1}{2}\right)^4 + 4\left(\frac{1}{2}\right)\left(\frac{1}{2}\right)^3 + 6\left(\frac{1}{2}\right)^2\left(\frac{1}{2}\right)^2 + 4\left(\frac{1}{2}\right)^3\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)^4 \end{aligned}$$

$$\text{No. of girls} = 240 \left[ \frac{1}{16} + \frac{4}{16} + \frac{6}{16} + \frac{4}{16} + \frac{1}{16} \right]$$

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$$= \frac{240 \times 1}{16} + \frac{240 \times 4}{16} + \frac{240 \times 6}{16} + \frac{240 \times 4}{16} + \frac{240 \times 1}{16}$$
$$= 15 + 60 + 90 + 60 + 15$$

These are the expected frequency of female births.

O	E	O - E	(O - E) <sup>2</sup>	$\frac{(O - E)^2}{E}$
10	15	-5	25	1.67
55	60	-5	25	0.41
105	90	15	225	2.5
58	60	-2	4	0.067
12	15	-3	9	0.6
			Total	5.247

Given  $\chi^2_{0.05} = 9.49$  &  $11.1$  for 4 d.f. and 5 d.f.  
Since the calculated value of  $\chi^2 (5.247) < \chi^2$   
value at 4 d.f. and 5 d.f.

Hence, the null hypothesis is accepted  
i.e., the male & female birth is  
equally probable.