

Derivation

- i) Consider a small section of an open channel. The forces acting on the free body of water ABCD in the direction of flow are as follow -
- i) Force of hydrostatic water pressure F_1 and F_2 acting on the two end of the free body

$$F_1 = F_2 \quad (\because \text{depth of water at section 1 \& 2 are same})$$

- ii) Component of weight of water in the direction of flow $wAL \sin \theta$

$$w = \text{Specific weight of water}$$

A = Wetted perimeter of the channel

θ = Angle of inclination of channel bottom with horizontal

(ii) The resistance of flow exerted by wetted surface of channel

P = Wetted perimeter of the channel

τ_0 = Average shear stresses at the channel boundary

Total resistance to flow = $PL\tau_0$

2) According Newton's second law of motion.

$$wAL \sin\theta - PL\tau_0 = 0$$

$$\tau_0 = w \left(\frac{A}{P} \right) \sin\theta = wRS_0 \quad \text{--- (1)}$$

$R = \frac{A}{P}$ Hydraulic radius

$S_0 = \sin\theta$ = slope of channel bottom

3) $\tau_0 = \frac{f}{8} \rho v^2$ --- (2)

4) Eq (1) & (2)

$$wRS_0 = \frac{f}{8} \rho v^2 =$$

$$v = \sqrt{\frac{8w}{f\rho} RS_0}$$

$$\sqrt{\frac{8g}{f}} \sqrt{RS_0}$$

$$g = w/p$$

$$v = c \sqrt{RS_0}$$

5) Discharge, $Q = AV = AC \sqrt{RS_0}$

$$C = \sqrt{\frac{8g}{f}}$$