

## SECTION 5

Q2

Ans

- (a) (i) Power set of  $\{a\} = \{\{\emptyset\}, \{a\}\}$   
(ii) Power set of  $\{a, b\} = \{\{\emptyset\}, \{a\}, \{b\}, \{a, b\}\}$   
(iii) Power set of  $\{\emptyset, \{\emptyset\}\} = \{\emptyset\}$   
(iv) Power set of  $\{a, \{a\}\} = \{\{\emptyset\}, \{a\}, \{\{a\}\}, \{a, \{a\}\}\}$

(b) Ring : A non-empty set  $R$  is a ring if it is equipped with two binary operations called addition and multiplication and denoted by '+' and '.' respectively i.e., for all  $a, b \in R$  we have  $a+b \in R$  and  $a \cdot b \in R$  and it satisfies the following properties:

(i) Addition is associative i.e.,  
 $(a+b)+c = a+(b+c) \forall a, b, c \in R$

(ii) Addition is commutative i.e.,  
 $a+b = b+a \forall a, b \in R$

(iii) There exists an element  $0 \in R$  such that  
 $0 + a = a = a + 0, \forall a \in R$

(iv) To each element  $a$  in  $R$  there exists an element  
 $-a$  in  $R$  such that  $a + (-a) = 0$

(v) Multiplication is associative i.e.,  
 $a \cdot (b \cdot c) = (a \cdot b) \cdot c, \forall a, b, c \in R$

(vi) Multiplication is distributive with respects to  
 addition i.e., for all  $a, b, c \in R$ ,

Example of ring with zero divisors:

$R = \{a \text{ set of } 2 \times 2 \text{ matrices}\}$ .

Field: A ring  $R$  with at least two elements  
 called a field if it has following properties:

- (i)  $R$  is commutative
- (ii)  $R$  has unity
- (iii)  $R$  is such that each non-zero element  
 possesses multiplicative inverse.

For example: The rings of real numbers and  
 complex numbers are also fields.