

Ans 2

$$\text{Maximize } z = 100x_1 + 40x_2$$

Subjected to

$$5x_1 + 2x_2 \leq 1000$$

$$3x_1 + 2x_2 \leq 900$$

$$x_1 + 2x_2 \leq 500$$

$$\text{and } x_1, x_2 \geq 0$$

Solution

(i) $5x_1 + 2x_2 \leq 1000$

Put $x_1 = 0$

Put $x_2 = 0$

$$0 + 2x_2 \leq 1000$$

$$5x_1 + 0 \leq 1000$$

$$x_2 \leq 500$$

$$x_1 \leq 200$$

(ii) $3x_1 + 2x_2 \leq 900$

Put $x_2 = 0$

Put $x_1 = 0$

$$3x_1 + 0 \leq 900$$

$$0 + 2x_2 \leq 900$$

$$x_1 \leq 300$$

$$x_2 \leq 450$$

(iii) $x_1 + 2x_2 \leq 500$

Put $x_2 = 0$

Put $x_1 = 0$

$$0 + x_1 \leq 500$$

$$0 + 2x_2 \leq 500$$

$$x_1 \leq 500$$

$$x_2 \leq 250$$

(iv) $x_1 + x_2 \geq 0$

Put $x_1 = 0$

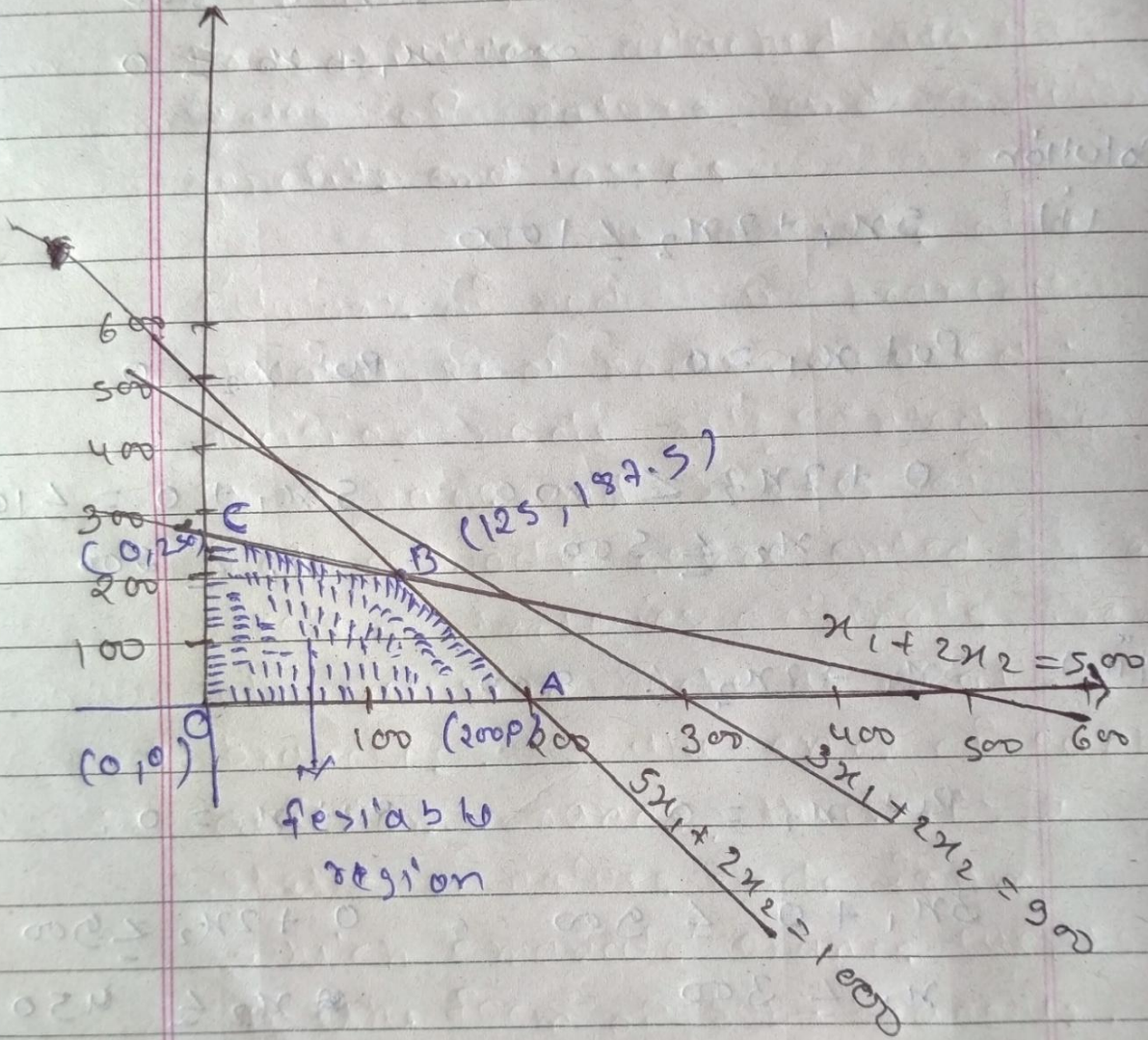
Put $x_2 = 0$

$0 + x_2 \geq 0$

$x_1 + 0 \geq 0$

$x_2 \geq 0$

$x_1 \geq 0$



The solution space is given by the feasible region OABC.

centre point	value $z = 100x_1 + 40x_2$
O (0, 0)	0
A (200, 0)	20,000
B (125, 187.5)	20,100 (Max value of z)
C (0, 250)	10,000

The maximum value of z occurs at two vertices A and B

since there are infinite no. of points on the line joining A and B gives the same maximum value of z . Thus, there are infinite no. of optimal solutions for the LPP.