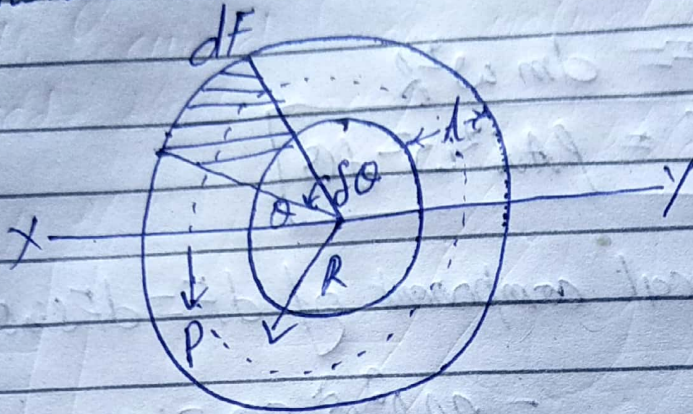


## Q.4 Dimensions of flywheel

Answer →



Consider a small element of rim which subtends an angle  $d\theta$  at the centre of the flywheel.

Let,  $D =$  Mean diameter of rim

$R =$  Mean radius of rim

$A =$  Cross-sectional area of rim

$v =$  Speed of flywheel

$\omega =$  Angular velocity of flywheel

$\sigma =$  Tensile stress due to centrifugal force

$v =$  Linear velocity at the mean radius

$$v = R\omega = \frac{\pi D N}{60}$$

Volume of the small element =  $AR d\theta$   
and, mass of the small element

$$dm = \text{density} \times \text{Volume}$$

$$dm = \rho AR d\theta$$

Centrifugal force that acts radially outwards

$$dF = dm \omega^2 r$$

$$dF = \rho A R^2 \omega^2 \delta \theta$$

vertical component of  $dF = dF \sin \theta$

$$= \rho A R^2 \omega^2 \delta \theta \sin \theta$$

Total vertical upward force tending to burst the rim.

$$F = \rho A R^2 \omega^2 \int_0^\pi \sin \theta d\theta = 2 \rho A R^2 \omega^2 \quad \text{--- (1)}$$

and

$$2 \rho A = 2 \rho A \sigma \quad \text{--- (2)}$$

on putting eq (1) and (2)

$$2 \rho A = 2 \rho A \sigma \omega^2$$

$$\sigma = \rho R^2 \omega^2$$

$$\sigma = \rho v^2$$

$$\sigma = \rho v^2$$

$$v = \sqrt{\frac{\sigma}{\rho}}$$

The mass of rim,  $m = \text{Volume} \times \text{Density}$   
 $= \pi D A P \quad \dots \dots \textcircled{3}$

and

$$A = \frac{m}{\pi D P} \quad \dots \dots \textcircled{4}$$

If the cross-sectional area of the rim is rectangular then

$$A = b t$$

$b =$  width of the rim

$t =$  thickness of the rim